

SECTION 'A'

Q.1 Choose the correct option.

- i. The function $y = 5 + x^4$ is a/an.....
 (A) Constant function (B) Even function (C) Odd function (D) Both even and odd function
- ii. $\lim_{x \rightarrow a} \frac{x^3 - a^3}{x - a} = \dots\dots\dots$
 (A) $3a$ (B) $2a^2$ (C) 0 (D) $3a^2$
- iii. If $f(x) = x^{100}$ then $f'(1) = \dots\dots\dots$
 (A) 100 (B) 99 (C) 50 (D) 0
- iv. $\frac{d}{dx} \left(\frac{1}{g(x)} \right) = \dots\dots\dots$
 (A) $\frac{g'(x)}{g(x)}$ (B) $\frac{-g'(x)}{(g(x))^2}$ (C) $\frac{-g'(x)}{g(x)}$ (D) $\frac{g'(x)}{(g(x))^2}$
- v. If $y = e^{2x}$ then y'' is equal to:
 (A) e^{2x} (B) $4e^{2x}$ (C) $2e^{2x}$ (D) xe^{2x}
- vi. $\int dx = \dots\dots\dots$
 (A) 1 (B) -1 (C) 0 (D) $x + c$
- vii. $\int (e^x + 1)dx = \dots\dots\dots$
 (A) $e^x + c$ (B) $e^x + x + c$ (C) $e^x + x^2 + c$ (D) $e^{2x} + 1 + c$
- viii. $\int \frac{f'(x)}{f(x)} dx = \dots\dots\dots$
 (A) $\ln|x| + c$ (B) $\ln|f(x)| + c$ (C) $\ln|f'(x)| + c$ (D) x^2
- ix. $\int x^{-1} dx = \dots\dots\dots$
 (A) $0 + c$ (B) $-x^2 + c$ (C) $\frac{x^{-2}}{0} + c$ (D) $\ln|x| + c$
- x. Solution of the differential equation $\frac{dy}{dx} = \sec^2 x$ is:
 (A) $y = \cos x + c$ (B) $y = \sec x + c$ (C) $y = \operatorname{cosec}^2 x + c$ (D) $y = \tan x + c$
- xi. The order of the differential equation $x \frac{d^2 y}{dx^2} + \left(\frac{dy}{dx} \right)^3 - 2 = 0$ is:
 (A) 3 (B) 2 (C) 1 (D) 0
- xii. Location of point $p(x, y)$ for which $x = y$ is in the quadrant:
 (A) 1^{st} & 3^{rd} (B) 1^{st} & 4^{th} (C) 2^{nd} & 4^{th} (D) 1^{st} & 2^{nd}
- xiii. Equation of a line passing through $(-2, 3)$ having a slope of 0 is :
 (A) $y=2$ (B) $y=-3$ (C) $y=3$ (D) $y = -2$
- xiv. A circle is called a point circle if :
 (A) $r=1$ (B) $r=-1$ (C) $r=0$ (D) $r=2$

- xv. The radius of the circle $(x - 3)^2 + (y - 2)^2 = 8$ is:
 (A) 8 (B) 64 (C) $2\sqrt{2}$ (D) 2
- xvi. Vertices of the ellipse $x^2 + 4y^2 = 16$ is :
 (A) $(\pm 4, 0)$ (B) $(0, \pm 4)$ (C) $(\pm 2, 0)$ (D) $(0, \pm 2)$
- xvii. Newton-Raphson method is _-----_ iterative method.
 (A) one point (B) Two points (C) Four points (D) There points
- xviii. Bisection Method is used to find.....
 (A) Real roots only (B) Imaginary roots (C) Differentiate function (D) Integrate function
- xix. If $f(x, y) = x^2y$ then $\frac{\partial f}{\partial x} = \dots\dots\dots$
 (A) $2x$ (B) $2xy$ (C) x^2 (D) x^2y
- xx. If $\vec{r} = \cos t \hat{i} + \sin t \hat{j} + \hat{k}$ then the velocity vector \vec{v} is:
 (A) $\sin t \hat{i} + \cos t \hat{j} + \hat{k}$ (B) $-\cos t \hat{i} + \cos t \hat{j}$ (C) $-\sin t \hat{i} + \cos t \hat{j}$ (D) $\sin t \hat{i} + \cos t \hat{j}$

SECTION 'B'

Marks 50

Q.2 Attempt Any TEN of the following short questions. Each question carries 5 marks.

- i. Evaluate: $\lim_{x \rightarrow 7} \frac{\sqrt{x}-\sqrt{7}}{x-7}$. (1+1+2+1=5)
- ii. Differentiate: $y = (3x^2 - 2) \cdot \sin x$ (1+2+2=5)
- iii. Use Maclaurin's series for $f(x) = \sin x$ (2+2+1=5)
- iv. Evaluate : $f(x) = \lim_{t \rightarrow 0} [\tan 2t \hat{i} + \ln(3 + t) \hat{j} + \hat{k}]$. (2+2+1=5)
- v. Evaluate: $\int_1^2 \frac{x}{x^2+2} dx$ (1+2+2=5)
- vi. Evaluate: $\int e^{2x} \cos 3x dx$. (2+2+1=5)
- vii. Write down an equation of the line which cuts the x-axis at (2,0) and y-axis at (0, -4). (2+2+1=5)
- viii. Find the area of the triangular region ABC whose vertices are A(1, 4), B(2, -3) and C(3,10). (2+2+1=5)
- ix. Find the center and radius of the circle $x^2 + y^2 + 12x - 10y = 0$ (1+2+2=5)
- x. Find an equation of the parabola whose focus is F(-3, 4) and directrix is $3x - 4y + 5 = 0$. (1+2+2=5)
- xi. Find an equation of the ellipse and its directories whose foci are $(\pm 2, 0)$ and eccentricity is $\frac{1}{2}$. (1+1+1+1+1=5)
- xii. Find general solution of $\frac{dy}{dx} + \cos 2x + 1 = 0$ (2+2+1=5)
- xiii. Solve up to four iteration of Newton-Raphson iterative method for $f(x) = \sin x, x_0 = -2$ (1+1+1+1+1=5)

SECTION 'C'

Marks 30

Note: Attempt Any Three questions. Each question carries 10 marks.

Q.3

- i. If $f(x) = \sqrt{x+4}$, then find $f(x^2 + 4)$. (1+2+2=5)
- ii. Use definition to find the derivative of $f(x) = x^2 + 2$. (1+2+2=5)

Q.4

- i. Find the area bounded by curve $y = 4 - x^2$ and the x-axis. (1+2+2=5)
- ii. Find an equation of the straight line if it is perpendicular to a line with slope -6 and its y-intercept is $\frac{4}{3}$. (2+2+1=5)

Q.5

- i. Find the equation of tangent and normal at the point $(-\sqrt{13}, \frac{9}{2})$ to the hyperbola $\frac{x^2}{4} - \frac{y^2}{9} = 1$. (2+2+1=5)
- ii. Find the equation of the circle whose center is (0, 0) and which contains the point(1, 2). (1+2+2=5)

Q.6

- i. Find the partial derivatives f_x and f_y of $f(x, y) = x^2 y^3 \tan^{-1} y$. (2+2+1=5)
- ii. Use the trapezoidal rule to approximate the value of $I = \int_1^3 x^2 dx$, $n = 6$. (1+2+2=5)